## FEDERAL UNIVERSITY OF TECHNOLOGY MINNA SCHOOL OF INFORMATION & COMMUNICATION TECHNOLOGY DEPARTMENT OF INFORMATION & MEDIA TECHNOLOGY SECOND SEMESTER EXAMINATION 2013/2014 SESSION **ICT 224: DISCRETE MATHEMATICS**

**INSTRUCTION:** ANSWER ANY FOUR (4) QUESTIONS TIME ALLOWED: 2 1/2 HRS

1. a) Let  $A = \{a, b, c\}$  and  $B = \{b, c, d, f, g\}$ , Find the following:

i)  $(A \cup B) - (A \cap B)$  ii)  $(A - B) \cup (B - A)$ 

iii)  $A \oplus B$ iv) |A|

b) Let  $A = \{a, b, c\}$ ,  $B = \{b, c, d\}$  and  $C = \{b, c, e\}$ . Show that A - (B - C) = (A - B) - C

c) Let  $P = \{1, 2, 3, 4, 5, 6\}$ ,  $P_1 = \{1, 2\}$ ,  $P_2 = \{3, 4\}$ ,  $P_3 = \{5, 6\}$ . Show that  $\{P_1, P_2, P_3\}$  is a partition of P.

2. a) Define the following terms:

i) Function

ii) Injective function

iii) Surjective function

iv) Inverse Relation

v) Inverse Function

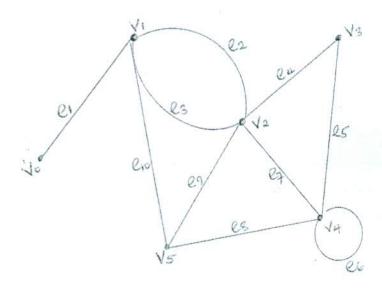
b) Let  $A = \{1, 2, 3\}$  and  $B = \{2, 3, 4\}$ . Let R and S be two binary relations defined from A to B as follows:  $(x, y) \in A \times B$ ,  $xRy \leftrightarrow 2/(x - y)$ 

 $(x, y) \in A \times B, (x, y) \in S \leftrightarrow x \ge y$ 

- i) Find R
- ii) Find S
- iii) Find  $R \cup S$
- c) Indicate whether any of the relations R or S in (2b) above is a function. If any, state the type of function, if not give reasons.
- 3. a) Let Z be the set of integers, show that congruence modulo 2 is an equivalent relation given that:  $x \equiv y \pmod{2}$  ("x is congruent to y modulo 2") if and only if x - y is even.
  - b) Let  $\mathbf{Z}^+$  be the set of non-negative integers and R the relation aRb if a divides b. Show that  $\mathbf{Z}^+$  is a poset.
  - c) Let  $A = \{a, b, c, d\}$  and  $R = \{(a, a), (b, c), (c, b), (d, d)\}$ .
  - i) Show that *R* is symmetric
  - ii) Show that *R* is not transitive.
- 4. a) Show that  $(r \lor p) \land [(\overline{r} \lor (p \land q)) \land (r \lor q)] \equiv p \land q$ .
  - b) Find the converse, inverse and contrapositive of the proposition "If n is prime, then n is odd or n is 2."

- c) Indicate which of the following propositions is a tautology, a contradiction or a contingency.
- i)  $(p \wedge \overline{q}) \wedge (\overline{p} \vee q)$

- ii)  $(p \wedge q) \vee (\overline{p \wedge q})$
- 5. a) Show that  $(\mathbb{Z}_2, +, ., \bar{}, 0, 1)$  is a Boolean algebra.
  - b) Draw a combinatorial circuit for the Boolean expression  $y = (x_1 + x_2).x_3$
  - c) Draw the logic table for the Boolean expression in (5b) above.
- 6. a) Consider the following graph G.



- i) Find  $E_G$ , and  $V_G$ ,
- ii) Find card(V) and card (E)
- iii) List the isolated vertices.

- iv) List the parallel edges.
- v) List the loops.
- vi) List the vertices adjacent to  $v_3$ .

- vii) List the vertices adjacent to  $v_2$ .
- viii) Find all edges incident on  $v_1$ .
- ix) Find the degree of vertex  $\,v_4\,$
- x) What type of graph is G?
- b) In the graph above, determine whether the following sequences are paths, or circuits.
  - i.  $v_0 e_1 v_1 e_{10} v_5 e_9 v_2 e_2 v_1$ .
- ii)  $v_1 e_2 v_2 e_3 v_1$ .
- iii)  $v_3 e_5 v_4 e_8 v_5 e_{10} v_1 e_3 v_2$ .
- iv)  $v_5 e_9 v_2 e_4 v_3 e_5 v_4 e_6 v_4 e_8 v_5$
- c) Draw a complete bipartite graph  $K_{4,3}$ .
- d) Define the following terms:
  - i. Simple graph.
- ii) Complete graph.
- iii)Pseudograph