

FEDERAL UNIVERSITY OF TECHNOLOGY MINNA, NIGERIA
SCHOOL OF ELECTRICAL ENGINEERING AND TECHNOLOGY
DEPARTMENT OF MECHATRONICS ENGINEERING
SECOND SEMESTER 2018/2019 B.Eng. DEGREE MID-SEMESTER EXAMINATION
COURSE: MCE 325(Signal Processing and Communication)
INSTRUCTION: Attempt All Questions
TIME ALLOWED: 2 Hours.

Question 1 (15 Marks)

Given the sequence of the two signals, $x[n]$ and $h[n]$, perform convolution on the given signals,

$$x[n] = [0 \ 0 \ 0 \ \underline{-2} \ 0 \ 1 \ -1 \ 3 \ 0 \ 0], \quad h[n] = [0 \ 0 \ 0 \ \underline{1} \ 2 \ 0 \ -1 \ 0 \ 0 \ 0], \quad \text{For } n \leq 7$$

- i. Using graphical method with appropriate equations and graphs. [8 Marks]
- ii. Using tabular method and plot all the necessary graphs. [7 Marks]

Question 2 (15 Marks)

Table 1 shows the data sequence obtained from a sensor, use the data to answer questions (i) to (iii)

Table 1:

N	0	1	2	3	4	5	6	7	8	9
x(n)	3	2	3	4	4	3	2	4	4	3

- a) Use the data to compute the output of a system given by
 - i. $y(n) = 0.2x(n) - 0.25x(n-1) - 0.5x(n-2)$ [3 Marks]
 - ii. $y(n) = 0.1y(n-1) - 0.03x(n-1) - 0.3x(n)$ [3 Marks]
 - iii. $y(n) = 0.1y(n-1) - 0.2y(n-2) - 0.3x(n) - 0.2x(n-1)$ [3 Marks]
- b) Plot $y(n)$ for each of the equations. [3 Marks]
- c) Draw the schematic Diagram for each of the equations. [3 Marks]

Question 3 (15 Marks)

a. Given

$$x(n) = \left(\frac{1}{5}\right)^n [u(n) - u(n-3)]$$

Determine $X(z)$ and its ROC [6 Marks]

b. The system characteristic equation is given by the difference equation
 $y(n) = 3.5y(n-1) - 1.5y(n-2) + x(n) - 5x(n-1) + 6x(n-2)$

- i) Determine the system transfer function. [3 Marks]

- ii) Determine the unit sample response of the system. [3 Marks]
- iii) Determine the response of the system to $x(n) = \delta(n) - 0.5\delta(n - 1)$
[3 Marks]

Question 4 (15 Marks)

- a. You are to design a causal discrete-time LTI system with the property that input is $x(n) = \left(\frac{1}{2}\right)^n u(n) - \frac{1}{4}\left(\frac{1}{2}\right)^{n-1}u(n - 1)$ and the output is $y(n) = \left(\frac{1}{3}\right)^n u(n)$
 - i. Determine the impulse $h(n)$ and the system function $H(z)$ of a system that satisfies the design conditions. [3 Marks]
 - ii. Find the difference equation that characterizes this system. [3 Marks]
 - iii. Determine a realization of the system that requires the minimum possible amount of memory. [3 Marks]
 - iv. Determine if the system is stable [2 Marks]
- b. Determine the zero-state response of the system $y(n) = \frac{1}{2}y(n - 1) + 4x(n) + 3x(n - 1)$ to the input $x(n) = e^{j\omega_0 n}u(n)$. What is the steady-state response of the system? [4 Marks]